

# Continuity of Translation Operators

Krishna B. Athreya, Justin R. Peters

(Submitted on 31 Oct 2010)

For a Radon measure  $\mu$  on  $\mathbb{R}$ , we show that  $L^{\infty}(\mu)$  is invariant under the group of translation operators  $T_t(f)(x) = \{f(x-t)\}$  ( $t \in \mathbb{R}$ ) if and only if  $\mu$  is equivalent to Lebesgue measure  $m$ . We also give necessary and sufficient conditions for  $L^p(\mu), 1 \leq p < \infty$ , to be invariant under the group  $\{T_t\}$  in terms of the Radon-Nikodym derivative w.r.t.  $m$ .

Comments: to appear, PAMS

Subjects: **Classical Analysis and ODEs (math.CA)**

MSC classes: primary: 26A42. secondary: 28A25, 22F10

Cite as: [arXiv:1011.0212v1](#) [math.CA]

## Submission history

From: Justin R. Peters [[view email](#)]

[v1] Sun, 31 Oct 2010 21:33:15 GMT (12kb)

[Which authors of this paper are endorsers?](#)

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

Current browse context:

**math.CA**

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1011](#)

Change to browse by:

[math](#)

## References & Citations

- [NASA ADS](#)

Bookmark([what is this?](#))

