

# On the finiteness of the Morse Index for Schrödinger operators

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Let  $H = \Delta + V$  be a Schrödinger on a complete non-compact manifold. It is known since the work of Fischer-Colbrie and Schoen that the finiteness of the negative spectrum of  $H$  implies the existence of a function  $\phi$  solution of  $H\phi = 0$  outside a compact set. This has consequences for minimal surfaces and for the finiteness of spaces of harmonic sections in the Bochner method. Here we show that the converse statement also holds: if there exists  $\phi$  solution of  $H\phi = 0$  outside a compact set, then  $H$  has a finite number of negative eigenvalues.

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