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# Squares in Polynomial Product Sequences

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Let  $F(n)$  be a polynomial of degree at least 2 with integer coefficients. We consider the products  $N_x = \prod_{1 \leq n \leq x} F(n)$  and show that  $N_x$  should only rarely be a perfect power. In particular, the number of  $x \leq X$  for which  $N_x$  is a perfect power is  $O(X^c)$  for some explicit  $c < 1$ . For certain  $F(n)$  we also prove that for only finitely many  $x$  will  $N_x$  be squarefull and, in the case of monic irreducible quadratic  $F(n)$ , provide an explicit bound on the largest  $x$  for which  $N_x$  is squarefull.

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