



Mathematics > Number Theory

Progress Towards Counting D_5 Quintic Fields

Eric Larson, Larry Rolen

(Submitted on 20 Jul 2011 (v1), last revised 6 Nov 2011 (this version, v4))

Let $N(5, D_5, X)$ be the number of quintic number fields whose Galois closure has Galois group D_5 and whose discriminant is bounded by X . By a conjecture of Malle, we expect that $N(5, D_5, X) \sim C X^{1/2}$ for some constant C . The best known upper bound is $N(5, D_5, X) \ll X^{3/4 + \epsilon}$, and we show this could be improved by counting points on a certain variety defined by a norm equation; computer calculations give strong evidence that this number is $\ll X^{2/3}$. Finally, we show how such norm equations can be helpful by reinterpreting an earlier proof of Wong on upper bounds for A_4 quartic fields in terms of a similar norm equation.

Comments: 7 pages
 Subjects: **Number Theory (math.NT)**
 MSC classes: 11R45, 11R29
 Cite as: [arXiv:1107.4111v4](https://arxiv.org/abs/1107.4111v4) [math.NT]

Submission history

From: Eric Larson [[view email](#)]
[\[v1\]](#) Wed, 20 Jul 2011 20:21:55 GMT (14kb,D)
[\[v2\]](#) Wed, 3 Aug 2011 16:35:16 GMT (14kb,D)
[\[v3\]](#) Mon, 8 Aug 2011 18:22:30 GMT (18kb,D)
[\[v4\]](#) Sun, 6 Nov 2011 01:42:35 GMT (14kb,D)

[Which authors of this paper are endorsers?](#)

Download:

- [PDF](#)
- [Other formats](#)

Current browse context:

math.NT
[< prev](#) | [next >](#)
[new](#) | [recent](#) | [1107](#)

Change to browse by:

[math](#)

References & Citations

- [NASA ADS](#)

Bookmark (what is this?)

