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On the L -series of F. Pellarin

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(Submitted on 25 Jul 2011 (v1), last revised 29 Dec 2011 (this version, v3))

The calculation, by L. Euler, of the values at positive even integers of the Riemann zeta function, in terms of powers of π and rational numbers, was a watershed event in the history of number theory and classical analysis. Since then many important analogs involving L -values and periods have been obtained. In analysis in finite characteristic, a version of Euler's result was given by L. Carlitz [\[ca2\]](#) in the 1930's which involved the period of a rank 1 Drinfeld module (the Carlitz module) in place of π . In a very original work [\[pe2\]](#), F. Pellarin has quite recently established a "deformation" of Carlitz's result involving certain L -series and the deformation of the Carlitz period given in [\[at1\]](#). Pellarin works only with the values of this L -series at positive integral points. We show here how the techniques of [\[go1\]](#) also allow these new L -series to be analytically continued -- with associated trivial zeroes -- and interpolated at finite primes.

Comments: In this version we show the entireness in terms of both x^{-1} and Pellarin's variable t in Theorem . To appear in the Journal of Number Theory volume in honor of David Hayes

Subjects: **Number Theory (math.NT)**

MSC classes: 11M38

Cite as: [arXiv:1107.5031](#) [math.NT]
(or [arXiv:1107.5031v3](#) [math.NT] for this version)

Submission history

From: David Goss [[view email](#)]

[\[v1\]](#) Mon, 25 Jul 2011 19:46:07 GMT (8kb)

[\[v2\]](#) Mon, 1 Aug 2011 20:30:44 GMT (8kb)

[\[v3\]](#) Thu, 29 Dec 2011 18:59:22 GMT (8kb)

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