

# Overpseudoprimes, and Mersenne and Fermat numbers as primover numbers

Vladimir Shevelev, Gilberto García-Pulgarín, Juan Miguel Velásquez-Soto, John H. Castillo

(Submitted on 4 Jun 2012)

We introduce a new class of pseudoprimes—so called "overpseudoprimes to base  $b$ ", which is a subclass of strong pseudoprimes to base  $b$ . Denoting via  $|b|_n$  the multiplicative order of  $b$  modulo  $n$ , we show that a composite  $n$  is overpseudoprime if and only if  $|b|_d$  is invariant for all divisors  $d > 1$  of  $n$ . In particular, we prove that all composite Mersenne numbers  $2^p - 1$ , where  $p$  is prime, are overpseudoprime to base 2 and squares of Wieferich primes are overpseudoprimes to base 2. Finally, we show that some kinds of well known numbers are overpseudoprime to a base  $b$ .

Comments: 9 pages

Subjects: **Number Theory (math.NT)**

MSC classes: 11A51 (Primary) 11A41, 11A07 (Secondary)

Cite as: [arXiv:1206.0606](https://arxiv.org/abs/1206.0606) [math.NT]

(or [arXiv:1206.0606v1](https://arxiv.org/abs/1206.0606v1) [math.NT] for this version)

## Submission history

From: John H. Castillo [[view email](#)]

[v1] Mon, 4 Jun 2012 13:06:15 GMT (8kb)

*Which authors of this paper are endorsers?*

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

## Current browse context:

math.NT

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1206](#)

## Change to browse by:

[math](#)

## References & Citations

- [NASA ADS](#)

## Bookmark (what is this?)



Science  
WISE