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# The Frattini Subalgebra of Restricted Lie Superalgebras

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**摘要** In the present paper, we study the Frattini subalgebra of a restricted Lie superalgebra  $(L, [p])$ . We show first that if  $L = A_1 \oplus A_2 \oplus \cdots \oplus A_n$ , then  $\phi_p(L) = \phi_p(A_1) + \phi_p(A_2) + \cdots + \phi_p(A_n)$ , where each  $A_i$  is a  $p$ -ideal of  $L$ . We then obtain two results:  $F(L) = \phi_p(L) = J(L) = L^{(1)}$  if and only if  $L$  is nilpotent;  $F_p(L)$  and  $F(L)$  are nilpotent ideals of  $L$  if  $L$  is solvable. In addition, necessary and sufficient conditions are found for  $\phi_p$ -free restricted Lie superalgebras. Finally, we discuss the relationships of  $\mathbb{F}$ - $p$ -restricted Lie superalgebras and  $\mathbb{F}$ -restricted Lie superalgebras.

**关键词** [restricted Lie superalgebras](#)  [\$\mathbb{F}\$ - \$p\$ -restricted Lie superalgebras](#) [Frattini  \$p\$ -subalgebra](#)  [\$\phi\_p\$ -free  \$p\$ -elementary](#)

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## The Frattini Subalgebra of Restricted Lie Superalgebras

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**Abstract** In the present paper, we study the Frattini subalgebra of a restricted Lie superalgebra  $(L, [p])$ . We show first that if  $L = A_1 \oplus A_2 \oplus \cdots \oplus A_n$ , then  $\phi_p(L) = \phi_p(A_1) + \phi_p(A_2) + \cdots + \phi_p(A_n)$ , where each  $A_i$  is a  $p$ -ideal of  $L$ . We then obtain two results:  $F(L) = \phi_p(L) = J(L) = L^{(1)}$  if and only if  $L$  is nilpotent;  $F_p(L)$  and  $F(L)$  are nilpotent ideals of  $L$  if  $L$  is solvable. In addition, necessary and sufficient conditions are found for  $\phi_p$ -free restricted Lie superalgebras. Finally, we discuss the relationships of  $\mathbb{F}$ - $p$ -restricted Lie superalgebras and  $\mathbb{F}$ -restricted Lie superalgebras.

**Key words** [restricted Lie superalgebras](#)  [\$\mathbb{F}\$ - \$p\$ -restricted Lie superalgebras](#) [Frattini  \$p\$ -subalgebra](#)  [\$\phi\_p\$ -free](#)  [\$p\$ -elementary](#)

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