



# Stratifications of derived categories from tilting modules over tame hereditary algebras

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In this paper, we consider the endomorphism algebras of infinitely generated tilting modules of the form  $R_{\mathcal{U}} \oplus R_{\mathcal{U}}/R$  over tame hereditary  $k$ -algebras  $R$  with  $k$  an arbitrary field, where  $R_{\mathcal{U}}$  is the universal localization of  $R$  at an arbitrary set  $\mathcal{U}$  of simple regular  $R$ -modules, and show that the derived module category of  $\text{End}_R(R_{\mathcal{U}} \oplus R_{\mathcal{U}}/R)$  is a recollement of the derived module category  $\mathcal{D}\{R\}$  of  $R$  and the derived module category  $\mathcal{D}\{\mathbb{A}_{\mathcal{U}}\}$  of the adèle ring  $\mathbb{A}_{\mathcal{U}}$  associated with  $\mathcal{U}$ . When  $k$  is an algebraically closed field, the ring  $\mathbb{A}_{\mathcal{U}}$  can be precisely described in terms of Laurent power series ring  $k((x))$  over  $k$ . Moreover, if  $\mathcal{U}$  is a union of finitely many cliques, we give two different stratifications of the derived category of  $\text{End}_R(R_{\mathcal{U}} \oplus R_{\mathcal{U}}/R)$  by derived categories of rings, such that the two stratifications are of different finite lengths.

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