

# On the Classification of Automorphic Lie Algebras

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It is shown that the problem of reduction can be formulated in a uniform way using the theory of invariants. This provides a powerful tool of analysis and it opens the road to new applications of these algebras, beyond the context of integrable systems. Moreover, it is proven that  $sl_2$ -Automorphic Lie Algebras associated to the icosahedral group  $I$ , the octahedral group  $O$ , the tetrahedral group  $T$ , and the dihedral group  $D_n$  are isomorphic. The proof is based on techniques from classical invariant theory and makes use of Clebsch-Gordan decomposition and transvectants, Molien functions and the trace-form. This result provides a complete classification of  $sl_2$ -Automorphic Lie Algebras associated to finite groups when the group representations are chosen to be the same and it is a crucial step towards the complete classification of Automorphic Lie Algebras.

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