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## The k-Derivation of a Gamma-Ring

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**Abstract:** In this paper, the k-derivation is defined on a  $\Gamma$ -ring M (that is, if M is a  $\Gamma$ -ring, d:M\to M and k: $\Gamma$  to  $\Gamma$  are to additive maps such that d(a $\beta$  b) = d(a) $\beta$  b + ak( $\beta$ )b + a $\beta$  d(b) for all a,b\in M, \quad  $\beta$  \in  $\Gamma$ , then d is called a k-derivation of M) and the following results are proved. (1) Let R be a ring of characteristic not equal to 2 such that if xry=0 for all x, y\in R then r=0. If d is a k-derivation of the (R=) $\Gamma$ ring R with k=d, then d is the ordinary derivation of R. (2) Let M be a nonzero prime  $\Gamma$ -ring of characteristic not equal to 2,  $\gamma$  be an element of  $\Gamma$  and a is an element in M such that [[x, a]<sub> $\gamma$ </sub>, a]<sub> $\gamma$ </sub> =0 for all x\in M. Then ay a = 0 or a\in C<sub>y</sub>. (3) Let M be a prime  $\Gamma$ -ring with CharM \ne 2, d be a nonzero kderivation of M,  $\gamma$  be a nonzero element of  $\Gamma$  and k( $\gamma$ ) \ne 0. If d(M) \subseteq C<sub> $\gamma$ </sub>, then M is a commutative

Key Words: k-derivation, derivation, commutativity, gamma-ring.