

# Turkish Journal of Mathematics

Turkish Journal

of

Mathematics

Finitary Actions and Invariant Ideals

D. S. PASSMAN

Department of Mathematics

University of Wisconsin

Madison, Wisconsin 53706, USA

e-mail: passman@math.wisc.edu

 [Keywords](#)  
 [Authors](#)



[math@tubitak.gov.tr](mailto:math@tubitak.gov.tr)

[Scientific Journals Home](#)  
[Page](#)

**Abstract:** Let  $K$  be a field and let  $G$  be a group. If  $G$  acts on an abelian group  $V$ , then it acts naturally on any group algebra  $K[V]$ , and we are concerned with classifying the  $G$ -stable ideals of  $K[V]$ . In this paper, we consider a rather concrete situation. We take  $G$  to be an infinite locally finite simple group acting in a finitary manner on  $V$ . When  $G$  is a finitary version of a classical linear group, then we show that the augmentation ideal  $\omega K[G]$  is the unique proper  $G$ -stable ideal of  $K[V]$ . On the other hand, if  $G$  is a finitary alternating group acting on a suitable permutation module  $V$ , then there is a rich family of  $G$ -stable ideals of  $K[V]$ , and we show that these behave like certain graded ideals in a polynomial ring.

**Key Words:** group algebra, invariant ideal, locally finite simple group, finitary permutation group, permutation module, finitary linear group

---

Turk. J. Math., **31**, (2007), 113-130.

Full text: [pdf](#)

Other articles published in the same issue: [Turk. J. Math., vol.31, iss. Suppl.](#)