



The Kaplansky condition and rings of almost stable range 1

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We present some variants of the Kaplansky condition for a K -Hermite ring R to be an elementary divisor ring; for example, a commutative K -Hermite ring R is an EDR iff for any elements $x, y, z \in R$ such that $(x, y) = (1)$, there exists an element $\lambda \in R$ such that $x + \lambda y = uv$, where $(u, z) = (v, 1 - z) = (1)$.

We present an example of a Bézout domain that is an elementary divisor ring, but it does not have almost stable range 1, thus answering a question of Warren Wm. McGovern.

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