



Homotopy categories and idempotent completeness, weight structures and weight complex functors

Olaf M. Schnürer

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This article provides some basic results on weight structures, weight complex functors and homotopy categories. We prove that the full subcategories $K(A)^{\{w < n\}}$, $K(A)^{\{w > n\}}$, $K(A)^{-}$ and $K(A)^{+}$ (of objects isomorphic to suitably bounded complexes) of the homotopy category $K(A)$ of an additive category A are idempotent complete, which confirms that $(K(A)^{\{w \leq 0\}}, K(A)^{\{w \geq 0\}})$ is a weight structure on $K(A)$. We discuss weight complex functors and provide full details of an argument sketched by M. Bondarko, which shows that if w is a bounded weight structure on a triangulated category T that has a filtered triangulated enhancement T' then there exists a strong weight complex functor $T \rightarrow K(\text{heart}(w))^{\text{anti}}$. Surprisingly, in order to carry out the proof, we need to impose an additional axiom on the filtered triangulated category T' which seems to be new.

Comments: 82 pages, comments welcome

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