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Fourier Restriction Estimates to Mixed **Homogeneous Surfaces**

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Abstract:

Let a, b be real numbers such that $2 \leq a < b$, and let $\varphi : \mathbb{R}^2 \to \mathbb{R}$ a mixed homogeneous function. We consider polynomial functions φ and also functions of the type $\varphi(x_1, x_2) = A |x_1|^a + B |x_2|^b$. Let

 $\Sigma = \{(x, \varphi(x)) : x \in B\}$ with the Lebesgue induced measure. For $f \in S(\mathbb{R}^3)$ and $x \in B$, let $(\mathcal{R}f)(x,\varphi(x)) = \widehat{f}(x,\varphi(x))$, where \widehat{f} denotes the usual Fourier transform.

For a large class of functions φ and for $1 \le p < \frac{4}{3}$ we characterize, up to endpoints, the pairs (p,q) such that $\mathcal R$ is a bounded operator from $L^{p}(\mathbb{R}^{3})$ on $L^{q}(\Sigma)$. We also give some sharp $L^{p} \to L^{2}$ estimates.



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