



# Global well-posedness and stability of electro-kinetic flows

Dieter Bothe, André Fischer, Jürgen Saal

(Submitted on 7 Jun 2012 (v1), last revised 9 Jun 2012 (this version, v2))

We consider a coupled system of Navier-Stokes and Nernst-Planck equations, describing the evolution of the velocity and the concentration fields of dissolved constituents in an electrolyte solution. Motivated by recent applications in the field of micro- and nanofluidics, we consider the model in such generality that electrokinetic flows are included. This prohibits employing the assumption of electroneutrality of the total solution, which is a common approach in the mathematical literature in order to determine the electrical potential. Therefore we complement the system of mass and momentum balances with a Poisson equation for the electrostatic potential, with the charge density stemming from the concentrations of the ionic species. For the resulting Navier-Stokes-Nernst-Planck-Poisson system we prove the existence of unique local strong solutions in bounded domains in  $\mathbb{R}^n$  for any  $n \geq 2$  as well as the existence of unique global strong solutions and exponential convergence to uniquely determined steady states in two dimensions.

Comments: 61 pages

Subjects: **Analysis of PDEs (math.AP)**

MSC classes: 76E25, 76D05, 35B25 (Primary) 35K51 (Secondary)

Cite as: **arXiv:1206.1457 [math.AP]**

(or **arXiv:1206.1457v2 [math.AP]** for this version)

## Submission history

From: Jürgen Saal [[view email](#)]

[v1] Thu, 7 Jun 2012 11:51:12 GMT (49kb)

[v2] Sat, 9 Jun 2012 07:06:45 GMT (49kb)

[Which authors of this paper are endorsers?](#)

Link back to: [arXiv](#), [form interface](#), [contact](#).

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

Current browse context:

math.AP

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1206](#)

Change to browse by:

[math](#)

## References & Citations

- [NASA ADS](#)

Bookmark [\(what is this?\)](#)

