



Nonlinear Sciences > Pattern Formation and Solitons

# Anisotropic covering of fractal sets

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We consider the optimal covering of fractal sets in a two-dimensional space using ellipses which become increasingly anisotropic as their size is reduced. If the semi-minor axis is  $\epsilon$  and the semi-major axis is  $\delta$ , we set  $\delta = \epsilon^\alpha$ , where  $0 < \alpha < 1$  is an exponent characterising the anisotropy of the covers. For point set fractals, in most cases we find that the number of points  $N$  which can be covered by an ellipse centred on any given point has expectation value  $\langle N \rangle \sim \epsilon^\beta$ , where  $\beta$  is a generalised dimension. We investigate the function  $\beta(\alpha)$  numerically for various sets, showing that it may be different for sets which have the same fractal dimension.

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