



# Sampling in Spaces of Bandlimited Functions on Commutative Spaces

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A connected homogeneous space  $X=G/K$  is called commutative if  $G$  is a connected Lie group,  $K$  is a compact subgroup and the  $B^*$ -algebra  $L^1(X)^K$  of  $K$ -invariant integrable function on  $X$  is commutative. In this article we introduce the space  $L^2_A(X)$  of  $A$ -bandlimited function on  $X$  by using the spectral decomposition of  $L^2(X)$ . We show that those spaces are reproducing kernel Hilbert spaces and determine the reproducing kernel. We then prove sampling results for those spaces using the smoothness of the elements in  $L^2_A(X)$ . At the end we discuss the example of  $R^d$ , the spheres  $S^d$ , compact symmetric spaces and the Heisenberg group realized as the commutative space  $U(n) \times H_n/U(n)$ .

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