



On the power-bounded operators of classes $C_{0 \cdot}$ and $C_{1 \cdot}$

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(Submitted on 3 Jun 2012)

By a bounded backward sequence of the operator T we mean a bounded sequence $\{x_n\}$ satisfying $Tx_{n+1} = x_n$. In [Pa] we have characterized contractions with strongly stable nonunitary part in terms of bounded backward sequences. The main purpose of this work is to extend that result to power-bounded operators. Additionally, we show that a power-bounded operator is strongly stable ($C_{0 \cdot}$) if and only if its adjoint does not have any nonzero bounded backward sequence. Similarly, a power-bounded operator is non-vanishing ($C_{1 \cdot}$) if and only if its adjoint has a lot of bounded backward sequences.

Subjects: **Functional Analysis (math.FA)**; Operator Algebras (math.OA)

MSC classes: 47A05, 47A45, 47B37, 47G10

Cite as: **arXiv:1206.0492 [math.FA]**
(or **arXiv:1206.0492v1 [math.FA]** for this version)

Submission history

From: Patryk Pagacz Mr. [[view email](#)]
[v1] Sun, 3 Jun 2012 21:34:52 GMT (7kb)

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