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Weighted Local Orlicz-Hardy Spaces with Applications to Pseudo-differential Operators

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Let Φ be a concave function on $(0, \infty)$ of strictly lower type $p_{\Phi} \in (0, 1]$ and $\omega \in A^{\{\mathop{\mathrm{loc}}\}_{\infty}}(\mathbb{R}^n)$. We introduce the weighted local Orlicz-Hardy space $h^{\{\Phi\}}_{\omega}(\mathbb{R}^n)$ via the local grand maximal function. Let $\rho(t) \equiv t^{-1} \wedge \Phi^{-1}(t^{-1})$ for all $t \in (0, \infty)$. We also introduce the $\mathop{\mathrm{BMO}}$ -type space $\mathop{\mathrm{bmo}}_{\rho, \omega}(\mathbb{R}^n)$ and establish the duality between $h^{\{\Phi\}}_{\omega}(\mathbb{R}^n)$ and $\mathop{\mathrm{bmo}}_{\rho, \omega}(\mathbb{R}^n)$. Several real-variable characterizations of $h^{\{\Phi\}}_{\omega}(\mathbb{R}^n)$ are presented. Using the atomic characterization, we prove the existence of finite atomic decompositions achieving the norm in some dense subspaces of $h^{\{\Phi\}}_{\omega}(\mathbb{R}^n)$. As applications, we show that the local Riesz transforms are bounded on $h^{\{\Phi\}}_{\omega}(\mathbb{R}^n)$, the local fractional integrals are bounded from $\|h^p_{\omega}(\mathbb{R}^n)\|$ to $\|L^q_{\omega}(\mathbb{R}^n)\|$ when $q > 1$ and from $\|h^p_{\omega}(\mathbb{R}^n)\|$ to $\|h^q_{\omega}(\mathbb{R}^n)\|$ when $q \leq 1$, and some pseudo-differential operators are also bounded on both $h^{\{\Phi\}}_{\omega}(\mathbb{R}^n)$. All results for any general Φ even when $\omega \equiv 1$ are new.

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