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## C*-algebras with the weak expectation property and a multivariable analogue of Ando's theorem on the numerical radius

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#### Abstract

A classic theorem of T. Ando characterises operators that have numerical radius at most one as operators that admit a certain positive $2 \times 2$ operator matrix completion. In this paper we consider variants of Ando's theorem, in which the operators (and matrix completions) are constrained to a given $\mathrm{C}^{*}$ algebra. By considering nxn matrix completions, an extension of Ando's theorem to a multivariable setting is made. We show that the $\mathrm{C}^{*}$-algebras in which these extended formulations of Ando's theorem hold true are precisely the $\mathrm{C}^{*}$-algebras with the weak expectation property (WEP). We also show that a $C^{*}$-subalgebra $A$ of $B(H)$ has WEP if and only if whenever a certain $3 \times 3$ (operator) matrix completion problem can be solved in matrices over $\mathrm{B}(\mathrm{H})$, it can also be solved in matrices over A. This last result gives a characterisation of WEP that is spatial and yet is independent of the particular representation of the $\mathrm{C}^{*}$-algebra. This leads to a new characterisation of injective von Neumann algebras. We also give a new equivalent formulation of the Connes Embedding Problem as a problem concerning $3 \times 3$ matrix completions.


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