



# An analysis of the practical DPG method

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In this work we give a complete error analysis of the Discontinuous Petrov Galerkin (DPG) method, accounting for all the approximations made in its practical implementation. Specifically, we consider the DPG method that uses a trial space consisting of polynomials of degree  $p$  on each mesh element. Earlier works showed that there is a "trial-to-test" operator  $\mathcal{T}$ , which when applied to the trial space, defines a test space that guarantees stability. In DPG formulations, this operator  $\mathcal{T}$  is local: it can be applied element-by-element. However, an infinite dimensional problem on each mesh element needed to be solved to apply  $\mathcal{T}$ . In practical computations,  $\mathcal{T}$  is approximated using polynomials of some degree  $r > p$  on each mesh element. We show that this approximation maintains optimal convergence rates, provided that  $r \geq p + N$ , where  $N$  is the space dimension (two or more), for the Laplace equation. We also prove a similar result for the DPG method for linear elasticity. Remarks on the conditioning of the stiffness matrix in DPG methods are also included.

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