

The asymptotic distribution of the length of Beta-coalescent trees

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We derive the asymptotic distribution of the total length L_n of a $\text{Beta}(2-\alpha, \alpha)$ -coalescent tree for $1 < \alpha < 2$, starting from n individuals. There are two regimes: If $\alpha \leq 1/2(1 + \sqrt{5})$, then L_n suitably rescaled has a stable limit distribution of index α . Otherwise L_n just has to be shifted by a constant (depending on n) to get convergence to a nondegenerate limit distribution. As a consequence, we obtain the limit distribution of the number S_n of segregation sites. These are points (mutations), which are placed on the tree's branches according to a Poisson point process with constant rate.

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