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# On Low-Dimensional Projections of High-Dimensional Distributions

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Let \$P\$ be a probability distribution on \$q\$-dimensional space. The socalled Diaconis-Freedman effect means that for a fixed dimension \$d << q\$, most \$d\$-dimensional projections of \$P\$ look like a scale mixture of spherically symmetric Gaussian distributions. The present paper provides necessary and sufficient conditions for this phenomenon in a suitable asymptotic framework with increasing dimension \$q\$. It turns out, that the conditions formulated by Diaconis and Freedman (1984) are not only sufficient but necessary as well. Moreover, letting \$\hat{P}\$ be the empirical distribution of \$n\$ independent random vectors with distribution \$P\$, we investigate the behavior of the empirical process \$\sqrt{n}(\hat{P} - P)\$ under random projections, conditional on \$\hat{P}\$.

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