



Mathematics > Combinatorics

# Fissioned triangular schemes via sharply 3-transitive groups

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n [D. de Caen, E.R. van Dam. Fissioned triangular schemes via the cross-ratio, {Europ. J. Combin.}, 22 (2001) 297-301], de Caen and van Dam constructed a fission scheme  $\text{FT}(q+1)$  of the triangular scheme on  $\text{PG}(1, q)$ . This fission scheme comes from the naturally induced action of  $\text{PGL}(2, q)$  on the 2-element subsets of  $\text{PG}(1, q)$ . The group  $\text{PGL}(2, q)$  is one of two infinite families of finite sharply 3-transitive groups. The other such family  $\text{Mq}(q)$  is a "twisted" version of  $\text{PGL}(2, q)$ , where  $q$  is an even power of an odd prime. The group  $\text{PSL}(2, q)$  is the intersection of  $\text{PGL}(2, q)$  and  $\text{Mq}(q)$ . In this paper, we investigate the association schemes coming from the actions of  $\text{PSL}(2, q)$ ,  $\text{Mq}(q)$  and  $\text{PML}(2, q)$ , respectively. Through the conic model introduced in [H.D.L. Hollmann, Q. Xiang. Association schemes from the actions of  $\text{PGL}(2, q)$  fixing a nonsingular conic, {J. Algebraic Combin.}, 24 (2006) 157-193], we introduce an embedding of  $\text{PML}(2, q)$  into  $\text{PML}(3, q)$ . For each of the three groups mentioned above, this embedding produces two more isomorphic association schemes: one on hyperbolic lines and the other on hyperbolic points (via a null parity) in a 3-dimensional orthogonal geometry. This embedding enables us to treat these three isomorphic association schemes simultaneously.

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