

# Some Quotients of the Boolean Lattice are Symmetric Chain Orders

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R. Canfield has conjectured that for all subgroups  $G$  of the automorphism group of the Boolean lattice  $B(n)$  (which can be regarded as the symmetric group  $S(n)$ ) the quotient order  $B(n)/G$  is a symmetric chain order. We provide a straightforward proof of a generalization of a result of K. K. Jordan: namely,  $B(n)/G$  is an SCO whenever  $G$  is generated by powers of disjoint cycles. The symmetric chain decompositions of Greene and Kleitman provide the basis for partitions of these quotients.

Comments: The significant changes from the first version are: inclusion of Theorem 3 and Corollary 1, with the proof of the former in Section 5. Small corrections and rewordings have been done as well

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