



# Graph bootstrap percolation

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Graph bootstrap percolation is a deterministic cellular automaton which was introduced by Bollobás in 1968, and is defined as follows. Given a graph  $H$ , and a set  $G \subset E(K_n)$  of initially 'infected' edges, we infect, at each time step, a new edge  $e$  if there is a copy of  $H$  in  $K_n$  such that  $e$  is the only not-yet infected edge of  $H$ . We say that  $G$  percolates in the  $H$ -bootstrap process if eventually every edge of  $K_n$  is infected. The extremal questions for this model, when  $H$  is the complete graph  $K_r$ , were solved (independently) by Alon, Kalai and Frankl almost thirty years ago. In this paper we study the random questions, and determine the critical probability  $p_c(n, K_r)$  for the  $K_r$ -process up to a poly-logarithmic factor. In the case  $r = 4$  we prove a stronger result, and determine the threshold for  $p_c(n, K_4)$ .

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