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Linear algebra and bootstrap percolation

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In \mathbb{H} -bootstrap percolation, a set $A \subset V(\mathbb{H})$ of initially 'infected' vertices spreads by infecting vertices which are the only uninfected vertex in an edge of the hypergraph \mathbb{H} . A particular case of this is the \mathbb{H} -bootstrap process, in which \mathbb{H} encodes copies of \mathbb{H} in a graph G . We find the minimum size of a set A that leads to complete infection when G and \mathbb{H} are powers of complete graphs and \mathbb{H} encodes induced copies of \mathbb{H} in G . The proof uses linear algebra, a technique that is new in bootstrap percolation, although standard in the study of weakly saturated graphs, which are equivalent to (edge) \mathbb{H} -bootstrap percolation on a complete graph.

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