



# Boxicity of graphs on surfaces

Louis Esperet, Gwenaël Joret

(Submitted on 11 Jul 2011 (v1), last revised 3 Jan 2012 (this version, v2))

The boxicity of a graph  $G=(V,E)$  is the least integer  $k$  for which there exist  $k$  interval graphs  $G_i=(V,E_i)$ ,  $1 \leq i \leq k$ , such that  $E=E_1 \cap \dots \cap E_k$ . Scheinerman proved in 1984 that outerplanar graphs have boxicity at most two and Thomassen proved in 1986 that planar graphs have boxicity at most three. In this note we prove that the boxicity of toroidal graphs is at most 7, and that the boxicity of graphs embeddable in a surface  $\Sigma$  of genus  $g$  is at most  $5g+3$ . This result yields improved bounds on the dimension of the adjacency poset of graphs on surfaces.

Comments: 9 pages, 2 figures

Subjects: **Combinatorics (math.CO)**

Cite as: **arXiv:1107.1953 [math.CO]**

(or **arXiv:1107.1953v2 [math.CO]** for this version)

## Submission history

From: Louis Esperet [[view email](#)]

[v1] Mon, 11 Jul 2011 07:35:32 GMT (39kb)

[v2] Tue, 3 Jan 2012 09:45:37 GMT (42kb)

*[Which authors of this paper are endorsers?](#)*

Link back to: [arXiv](#), [form interface](#), [contact](#).

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

Current browse context:

math.CO

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1107](#)

Change to browse by:

[math](#)

## References & Citations

- [NASA ADS](#)

Bookmark([what is this?](#))

