



# The local $h$ -vector of the cluster subdivision of a simplex

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The cluster complex  $\Delta(\Phi)$  is an abstract simplicial complex, introduced by Fomin and Zelevinsky for a finite root system  $\Phi$ . The positive part of  $\Delta(\Phi)$  naturally defines a simplicial subdivision of the simplex on the vertex set of simple roots of  $\Phi$ . The local  $h$ -vector of this subdivision, in the sense of Stanley, is computed and the corresponding  $\gamma$ -vector is shown to be nonnegative. Combinatorial interpretations to the entries of the local  $h$ -vector and the corresponding  $\gamma$ -vector are provided for the classical root systems, in terms of noncrossing partitions of types  $A$  and  $B$ . An analogous result is given for the barycentric subdivision of a simplex.

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