

Original Articles

# On the Stabilizer of the Automorphism Group of a 4-valent Vertex-transitive Graph with Odd-prime-power Order

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**摘要** Let  $X$  be a 4-valent connected vertex-transitive graph with odd-prime-power order  $p \sim k$  ( $k \geq 1$ ), and let  $A$  be the full automorphism group of  $X$ . In this paper, we prove that the stabilizer  $A_v$  of a vertex  $v$  in  $A$  is a 2-group if  $p \neq 5$ , or a  $\{2,3\}$ -group if  $p = 5$ . Furthermore, if  $p = 5$   $|A_v|$  is not divisible by  $3 \sim 2$ . As a result, we show that any 4-valent connected vertex-transitive graph with odd-prime-power order  $p \sim k$  ( $k \geq 1$ ) is at most 1-arc-transitive for  $p \neq 5$  and 2-arc-transitive for  $p = 5$ .

**关键词** [cayley graphs](#) [s](#) [-arc-transitive](#) [vertex-transitive](#)

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**Key words** [cayley graphs](#) [s](#) [-arc-transitive](#) [vertex-transitive](#)

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