

Original Articles

Generalized Steiner Triple systems with Group Size $g \equiv 0, 3 \pmod{6}$

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摘要 Generalized Steiner triple systems, $(GS(2,3,n,g))$, are equivalent to maximum constant weight codes over an alphabet of size $g+1$ with distance 3 and weight 3 in which each codeword has length n . The necessary conditions for the existence of a $GS(2,3,n,g)$ are $(n-1)g \equiv 0 \pmod{2}$, $n(n-1)g \equiv 2 \pmod{6}$, and $n \geq g+2$. These necessary conditions are shown to be sufficient by several authors for $2 \leq g \leq 11$. In this paper, three new results are obtained. First, it is shown that for any given g , $g \equiv 0 \pmod{6}$ and $g \geq 12$, if there exists a $GS(2,3,n,g)$ for all n , $g+2 \leq n \leq 7g+13$, then the necessary conditions are also sufficient. Next, it is also shown that for any given g , $g \equiv 3 \pmod{6}$ and $g \geq 15$, if there exists a $GS(2,3,n,g)$ for all n , $n \equiv 1 \pmod{2}$ and $g+2 \leq n \leq 7g+6$, then the necessary conditions are also sufficient. Finally, as an application, it is proved that the necessary conditions for the existence of a $GS(2,3,n,g)$ are also sufficient for $g=12, 15$.

关键词 [generalized steiner triple system](#) [constant weight codes](#)

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Abstract Generalized Steiner triple systems, $(GS(2,3,n,g))$, are equivalent to maximum constant weight codes over an alphabet of size $g+1$ with distance 3 and weight 3 in which each codeword has length n . The necessary conditions for the existence of a $GS(2,3,n,g)$ are $(n-1)g \equiv 0 \pmod{2}$, $n(n-1)g \equiv 2 \pmod{6}$, and $n \geq g+2$. These necessary conditions are shown to be sufficient by several authors for $2 \leq g \leq 11$. In this paper, three new results are obtained. First, it is shown that for any given g , $g \equiv 0 \pmod{6}$ and $g \geq 12$, if there exists a $GS(2,3,n,g)$ for all n , $g+2 \leq n \leq 7g+13$, then the necessary conditions are also sufficient. Next, it is also shown that for any given g , $g \equiv 3 \pmod{6}$ and $g \geq 15$, if there exists a $GS(2,3,n,g)$ for all n , $n \equiv 1 \pmod{2}$ and $g+2 \leq n \leq 7g+6$, then the necessary conditions are also sufficient. Finally, as an application, it is proved that the necessary conditions for the existence of a $GS(2,3,n,g)$ are also sufficient for $g=12, 15$.

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