

平面负位势相关的Schrodinger方程的广义Picard原理

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摘要 设 β 是复平面上圆盘 $\Omega_\alpha = \{z \mid |z| < \alpha\}$ 内的一个零容紧致集.考虑 $\Omega \sim \beta_\alpha = \Omega_\alpha \setminus \beta$ 上的定常Schr [AKo] dinger方程 $(-\Delta + \mu)u = 0$,其中位势 $\mu \leq 0$ 是Kato类Radon测度.方程在广义函数意义下的连续解称为 μ -调和函数.将在 $\{z \mid |z| = \alpha\}$ 上取极限值0的非负 μ -调和函数族记为 $_{\mu}H$.对 $\Omega \sim \beta_\alpha$ 的Kerekjato-Stoilow意义下的理想边界 β 的任一点 ζ .该文通过定义 $_{\mu}H \rightarrow _{\mu}H$ 的线性算子 π_ζ ,引入 $_{\mu}H$ 的子函数族 $H_\zeta = \{u \in _{\mu}H \mid \pi_\zeta(u) = 0\}$,证明了在 $\Omega \sim \beta_\alpha$ 上关于 ζ 的 μ -广义Picard原理成立,即 $_{\mu}H$ 的维数是1或 $_{\mu}H/H_\zeta$ 的维数是1二者必居其中.

关键词 [Schr dinger方程](#), [广义函纹](#), [Sobolev空间](#), [Picard原理](#)

分类号

GENERALIZED PICARD PRINCIPLE FOR SCHR DINGER EQUATIONS WITH NEGATIVE PLANAR POTENTIALS

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Abstract Let β be a compact set with null capacity in the disc $\Omega_\alpha = \{z \mid |z| < \alpha\}$ on the complex plane. Consider a stationary Schr [AKo] dinger equation $(-\Delta + \mu)u = 0$, where the potential $\mu \leq 0$ is a Radon measure of Kato Class on $\Omega \sim \beta_\alpha = \Omega_\alpha \setminus \beta$. Denote by $_{\mu}H$ the class of all functions u on $\Omega \sim \beta_\alpha$ with the following properties: u is nonnegative and continuous on $\Omega \sim \beta_\alpha$; u vanishes on $\{z \mid |z| = \alpha\}$; u is a distributional solution of the equation on $\Omega \sim \beta_\alpha$. For an ideal boundary point $\zeta \in \beta$ of $\Omega \sim \beta_\alpha$ in Kerekjato-Stoilow's sense, a linear operator π_ζ of $_{\mu}H \rightarrow _{\mu}H$ is defined, and a subclass $H_\zeta = \{u \in _{\mu}H \mid \pi_\zeta(u) = 0\}$ of $_{\mu}H$ is introduced. It is proved that the μ -generalized Picard principle is valid for ζ on $\Omega \sim \beta_\alpha$, i.e., one of the following statements is true: (i) $_{\mu}H$ is of dimension 1, and (ii) $_{\mu}H/H_\zeta$ is of dimension 1.

Key words [Distribution](#) [Sobolev space](#) [Brelot space](#) [Generalized Picard principle](#)

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