

非线性项依赖一阶导数共振情形下二阶三点BVP解的存在唯一性

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Existence and Uniqueness of Three-point Boundary Value Problem at Resonance with Nonlinear Term Depending on the First Order Derivative

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摘要 本文致力于研究共振情形下二阶三点边值问题 $x''(t)+f(t,x(t),x'(t))=0, t \in (0,1), x(0)=0, x(1)=\xi x(\eta)$, 其中 $f: [0,1] \times \mathbb{R}^2 \rightarrow \mathbb{R}$ 是一个连续函数, $\xi > 0, 0 < \eta < 1$ 满足 $\xi\eta=1$. 运用先验界估计, 微分不等式技巧和Leray-Schauder度理论得到了该边值问题解的存在性和唯一性.

关键词: 非线性边值问题 存在性和唯一性 共振 上下解 Leray-Schauder度

Abstract: This paper is devoted to studying the second-order three point boundary value problem at resonance $x''(t)+f(t,x(t),x'(t))=0, t \in (0,1),$

$x(0)=0, x(1)=\xi x(\eta)$, where $f: [0,1] \times \mathbb{R}^2 \rightarrow \mathbb{R}$ is continuous, $\xi > 0, 0 < \eta < 1$ such that $\xi\eta=1$. The existence and uniqueness of solution of the boundary value problem are given by using priori estimates, differential inequalities technique and Leray-Schauder degree theory.

Key words: nonlinear boundary value problem existence and uniqueness resonance upper and lower solutions Leray-Schauder degree

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