

## 弱拟法锥条件下非凸优化问题的同伦算法

刘庆怀<sup>1</sup>, 张春阳<sup>2</sup>, 张树功<sup>2</sup>

1. 长春工业大学应用数学所, 长春 130012;
2. 吉林大学数学研究所, 长春 130012

## Homotopy Method for Solving Nonconvex Optimization with Weak Quasi Normal Condition

LIU Qinghuai<sup>1</sup>, ZHANG Chunyang<sup>2</sup>, ZHANG Shugong<sup>2</sup>

1. Institute of Applied Mathematics, Changchun University of Technology, Changchun 130012;
2. Institute of mathematics, Jilin University, Changchun 130012

- [摘要](#)
- [参考文献](#)
- [相关文章](#)

全文: [PDF \(368 KB\)](#) [HTML \(1 KB\)](#) 输出: [BibTeX](#) | [EndNote \(RIS\)](#) [背景资料](#)

**摘要** 本文给出弱拟法锥条件的定义, 并针对非线性组合同伦方程, 得到在弱拟法锥条件下求解约束非凸优化问题的同伦内点算法. 证明了该算法对于可行域的某个子集中几乎所有的点, 同伦路径存在, 并且同伦路径收敛于问题的K-K-T点. 通过数值例子验证了该算法是有效的.

**关键词:** [非凸优化](#) [同伦算法](#) [内点法](#) [弱拟法锥条件](#)

**Abstract:** In this paper, we define the weak quasi-normal cone condition and consider the nonlinear homotopy equation under the weak quasi-normal cone condition to solve constrained non-convex programming program. For almost all the point in some feasible sub-set, the existence of the homotopy path is proved and the homotopy path converges to the K-K-T point. Numerical examples are presented to show the effectiveness of the algorithm.

**Key words:** [nonconvex optimization](#) [homotopy method](#) [interior point method](#) [weak quasi-normal cone condition](#)

收稿日期: 2006-01-09;

基金资助:

国家自然科学基金资助项目(10771020), 吉林省自然科学基金资助项目(20101597).

引用本文:

. 弱拟法锥条件下非凸优化问题的同伦算法[J]. 应用数学学报, 2011, 34(6): 996-1006.

. Homotopy Method for Solving Nonconvex Optimization with Weak Quasi Normal Condition[J]. Acta Mathematicae Applicatae Sinica, 2011, 34(6): 996-1006.

- [1] Carcia C B, Zangwill W I. Pathways to Solutions, Fixed Points, and Equilibria. Prentice-Hall, 1981
- [2] Karmarkar N. A New Polynomial-time Algorithm for Linear Programming. Com-binatorica, 1984, 4(4): 373-395
- [3] Feng Guochen, Yu Bo. Combined Homotopy Interior Point Method for Nonlinear Programming Problems. Lecture Notes in Num. Anal., 1995, 14: 9-16
- [4] Feng Guochen, Lin Zhenghua, Yu Bo. Existence of an Interior Pathway to a Karush-Kuhn-Tucker Point of a Nonconvex Programming Problem. J. Nonlinear Analysis, 1998, 32: 761-768 
- [5] Lin Zhenghua, Yu Bo, Feng Guo-chen. Combined Homotopy Interior Point Method for Convex Nonlinear Programming. J. Appl. Math.

## 服务

- ▶ [把本文推荐给朋友](#)
- ▶ [加入我的书架](#)
- ▶ [加入引用管理器](#)
- ▶ [E-mail Alert](#)
- ▶ [RSS](#)

## 作者相关文章

- [6] Lin Zhenghua, Li Yong, Yu Bo. A Combined Homotopy Interior Point Method for General Nonlinear Programming Problems. *J. Appl. Math. Comput.*, 1996, 80: 209-224 
- [7] Xiong Huijuan, Yu Bo. An Aggregate Deformation Homotopy Method for Constrained Min-max-min Problems with Max-min Constraints. *J. Computational Optimization and Applications*, 2009, DOI 10.1007/s10589-008-9229-y
- [8] Yu Bo, Feng G C, Zhang S L. The Aggregate Constraint Homotopy Method for Nonconvex Nonlinear Programming. *J. Nonlinear Analysis, TMA*, 2001, 45: 839-847 
- [9] Liu Qinghuai, Yu Bo, Feng Guo-chen. An Interior Point Path-following Method for Nonconvex Programming with Quasi Normal Cone Condition. *Advances in Mathematics of Communication*, 2000, 29: 281-282
- [10] Xiaona Fan, Yu Bo. Homotopy Method for Solving Variational Inequalities with Bounded Box Constraints. *Nonlinear Analysis*, 2008, 8 (68): 2357-2361
- [11] Xiaona Fan, Yu Bo. A Smoothing Homotopy Method for Solving Variational Inequalities. *Nonlinear Analysis*, 2009, 1(70): 211-219
- [12] Yu Qian, Huang Chongchao, Wang Xianjia. A Combined Homotopy Interior Point Method for the linear Complementarity Problem. *Applied Mathematics and Computation*, 2006, 2(179): 696-701
- [13] Su Menglong, Liu Zhenxin. Modified Homotopy Methods to Solve Fixed Points of Self-mapping in a Broader Class of Nonconvex Sets. *Applied Numerical Mathematics*, 2008, 3(58): 236-248
- [14] Sun Wenjuan, Wang Cailing, Liu Qinghuai. A Homotopy Method for Getting a Local Minimum of Constrained Nonconvex Programming. *Nonlinear Analysis*, 2009, 71(10): 4725-4731 
- [15] 刘庆怀, 于波, 冯果忱. 基于拟法锥条件的非凸非线性规划问题的同伦内点法. *应用数学学报*, 2003, 26(2): 372-373 (Liu Qinghuai, Yu Bo, Feng Guochen. A Homotopy Interior Method for Solving Nonlinear Nonconvex Programming with Quasi Normal Cone Condition. *Acta Mathematicae Applicatae Sinica*, 2003, 26(2): 372-373) 浏览
  
- [1] 李向利, 刘红卫, 黄亚魁. 求解特定线性互补问题的牛顿KKT内点法[J]. *应用数学学报*, 2010, 33(5): 889-899.
- [2] 李向利, 刘红卫, 黄亚魁. 求解特定线性互补问题的牛顿KKT内点法[J]. *应用数学学报*, 2010, 33(1): 889-899.
- [3] 刘庆怀, 林正华. 求解多目标规划最小弱有效解的同伦内点方法[J]. *应用数学学报*, 2000, 23(2): 188-195.