

## 误差为FCA过程的线性模型HD估计的渐近正态性

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## Asymptotic Normality of HD Estimators for Linear Models with Functional Coefficient Autoregressive Processes

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**摘要** 考虑线性回归模型  $y = x^T \beta + e$ , 其中误差  $e$  是函数系数自回归(FCA)过程. 本文研究该模型未知参数的 Huber-Dutter 估计的渐近性质, 在合理的条件下, 证明了这些估计量以  $n^{-1/2}$  速度渐近于正态分布.

**关键词:** [线性回归模型](#) [函数系数自回归过程](#) [HD估计](#) [正态分布](#)

**Abstract:** Consider the following linear regression model  $y = x^T \beta + e$ , where the error  $e$  is a functional coefficient autoregressive (FCA) processes. In this paper we investigate asymptotic behavior of Huber-Dutter (HD) estimators for unknown parameters in the above model. Under some regular conditions, it is shown that the HD estimators are asymptotically normal with convergence rate  $n^{-1/2}$  by the using of martingale difference technique.

**Key words:** [linear regression model](#) [functional coefficient autoregressive process](#) [Huber-Dutter estimators](#) [normal distribution](#)

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