

The dimension of ergodic random sequences

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Let μ be a computable ergodic shift-invariant measure over the Cantor space. Providing a constructive proof of Shannon-McMillan-Breiman theorem, V'yugin proved that if a sequence x is Martin-Löf random w.r.t. μ then the strong effective dimension $\text{Dim}(x)$ of x equals the entropy of μ . Whether its effective dimension $\text{dim}(x)$ also equals the entropy was left as an open question. In this paper we settle this problem, providing a positive answer. A key step in the proof consists in extending recent results on Birkhoff's ergodic theorem for Martin-Löf random sequences.

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