



# A computability challenge: asymptotic bounds and isolated error-correcting codes

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Consider the set of all error--correcting block codes over a fixed alphabet with  $q$  letters. It determines a recursively enumerable set of points in the unit square with coordinates  $(R, \delta) := \{ \text{it (relative transmission rate, relative minimal distance).} \}$  Limit points of this set form a closed subset, defined by  $R \leq \alpha_q(\delta)$ , where  $\alpha_q(\delta)$  is a continuous decreasing function called *asymptotic bound*. Its existence was proved by the author in 1981, but all attempts to find an explicit formula for it so far failed. In this note I consider the question whether this function is computable in the sense of constructive mathematics, and discuss some arguments suggesting that the answer might be negative.

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