



Mathematical Physics

Notes on Ding-Iohara algebra and AGT conjecture

H. Awata, B. Feigin, A. Hoshino, M. Kanai, J. Shiraishi, S. Yanagida

(Submitted on 21 Jun 2011 (v1), last revised 7 Jul 2011 (this version, v3))

We study the representation theory of the Ding-Iohara algebra \mathcal{U} to find q -analogues of the Alday-Gaiotto-Tachikawa (AGT) relations. We introduce the endomorphism $T(u,v)$ of the Ding-Iohara algebra, having two parameters u and v . We define the vertex operator $\Phi(w)$ by specifying the permutation relations with the Ding-Iohara generators $x^{\pm}(z)$ and $\psi^{\pm}(z)$ in terms of $T(u,v)$. For the level one representation, all the matrix elements of the vertex operators with respect to the Macdonald polynomials are factorized and written in terms of the Nekrasov factors for the K -theoretic partition functions as in the AGT relations. For higher levels $m=2,3,\dots$, we present some conjectures, which imply the existence of the q -analogues of the AGT relations.

Comments: 21 pages; Proceeding of RIMS Conference 2010 "Diversity of the Theory of Integrable Systems" (ed. Masahiro Kanai)

Subjects: **Mathematical Physics (math-ph)**; High Energy Physics - Theory (hep-th); Quantum Algebra (math.QA)

Cite as: **arXiv:1106.4088 [math-ph]**
(or **arXiv:1106.4088v3 [math-ph]** for this version)

Submission history

From: Masahiro Kanai [[view email](#)]

[v1] Tue, 21 Jun 2011 04:55:23 GMT (24kb)

[v2] Mon, 27 Jun 2011 09:56:34 GMT (24kb)

[v3] Thu, 7 Jul 2011 05:29:37 GMT (24kb)

Which authors of this paper are endorsers?

Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

Current browse context:

math-ph

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1106](#)

Change to browse by:

[hep-th](#)

[math](#)

[math.QA](#)

References & Citations

- [NASA ADS](#)

Bookmark (what is this?)

