

## Mathematical Physics

# Haag duality and the distal split property for cones in the toric code

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We prove that Haag duality holds for cones in the toric code model. That is, for a cone  $\Lambda$ , the algebra  $R_\Lambda$  of observables localized in  $\Lambda$  and the algebra  $R_{\Lambda^c}$  of observables localized in the complement  $\Lambda^c$  generate each other's commutant as von Neumann algebras. Moreover, we show that the distal split property holds: if  $\Lambda_1 \subset \Lambda_2$  are two cones whose boundaries are well separated, there is a Type I factor  $N$  such that  $R_{\Lambda_1} \subset N \subset R_{\Lambda_2}$ . We demonstrate this by explicitly constructing  $N$ .

Comments: 15 pages, 2 figures, v2: extended introduction

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