



Mathematical Physics

# Essential variational Poisson cohomology

Alberto De Sole, Victor G. Kac

(Submitted on 29 Jun 2011)

In our recent paper [DSK11] we computed the dimension of the variational Poisson cohomology for any quasicontant coefficient matrix differential operator  $K$  of arbitrary order with invertible leading coefficient, provided that the algebra of differential functions is normal and is an algebra over a linearly closed differential field. In the present paper we show that, for  $K$  skewadjoint, this cohomology, viewed as a  $\mathbb{Z}$ -graded Lie superalgebra, is isomorphic to the finite dimensional Lie superalgebra of Hamiltonian vector fields over a Grassman algebra. We also prove that the subalgebra of 'essential' variational Poisson cohomology, consisting of classes vanishing on the Casimirs of  $K$ , is zero. This vanishing result has applications to the theory of bi-Hamiltonian structures and their deformations. At the end of the paper we consider also the translation invariant case.

Comments: 30 pages  
 Subjects: **Mathematical Physics (math-ph)**; Representation Theory (math.RT)  
 MSC classes: 37K10 (Primary) 37K30, 17B80 (Secondary)  
 Journal reference: Communications in Mathematical Physics: Volume 313, Issue 3 (2012), Page 837-864  
 DOI: [10.1007/s00220-012-1461-8](https://doi.org/10.1007/s00220-012-1461-8)  
 Cite as: [arXiv:1106.5882](https://arxiv.org/abs/1106.5882) [math-ph]  
 (or [arXiv:1106.5882v1](https://arxiv.org/abs/1106.5882v1) [math-ph] for this version)

## Submission history

From: Alberto De Sole [[view email](#)]  
 [v1] Wed, 29 Jun 2011 09:11:21 GMT (28kb)

*Which authors of this paper are endorsers?*

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

## Current browse context:

math-ph  
[< prev](#) | [next >](#)  
[new](#) | [recent](#) | [1106](#)

## Change to browse by:

[math](#)  
[math.RT](#)

## References & Citations

- [NASA ADS](#)

## Bookmark (what is this?)

