

General Relativity and Quantum Cosmology

Three-dimensional gravity and Drinfel'd doubles: spacetimes and symmetries from quantum deformations

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We show how the constant curvature spacetimes of 3d gravity and the associated symmetry algebras can be derived from a single quantum deformation of the 3d Lorentz algebra $sl(2, \mathbb{R})$. We investigate the classical Drinfel'd double of a "hybrid" deformation of $sl(2, \mathbb{R})$ that depends on two parameters (η, z) . With an appropriate choice of basis and real structure, this Drinfel'd double agrees with the 3d anti-de Sitter algebra. The deformation parameter η is related to the cosmological constant, while z is identified with the inverse of the speed of light and defines the signature of the metric. We generalise this result to de Sitter space, the three-sphere and 3d hyperbolic space through analytic continuation in η and z ; we also investigate the limits of vanishing η and z , which yield the flat spacetimes (Minkowski and Euclidean spaces) and Newtonian models, respectively.

Comments: 12 pages; minor changes, additional references

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