



High Energy Physics - Phenomenology

# Numerical solution of $Q^2$ evolution equations for fragmentation functions

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Semi-inclusive hadron-production processes are becoming important in high-energy hadron reactions. They are used for investigating properties of quark-hadron matters in heavy-ion collisions, for finding the origin of nucleon spin in polarized lepton-nucleon and nucleon-nucleon reactions, and possibly for finding exotic hadrons. In describing the hadron-production cross sections in high-energy reactions, fragmentation functions are essential quantities. A fragmentation function indicates the probability of producing a hadron from a parton in the leading order of the running coupling constant  $\alpha_s$ . Its  $Q^2$  dependence is described by the standard DGLAP (Dokshitzer-Gribov-Lipatov-Altarelli-Parisi) evolution equations, which are often used in theoretical and experimental analyses of the fragmentation functions and in calculating semi-inclusive cross sections. The DGLAP equations are complicated integro-differential equations, which cannot be solved in an analytical method. In this work, a simple method is employed for solving the evolution equations by using Gauss-Legendre quadrature for evaluating integrals, and a useful code is provided for calculating the  $Q^2$  evolution of the fragmentation functions in the leading order (LO) and next-to-leading order (NLO) of  $\alpha_s$ . The renormalization scheme is  $\overline{\text{MS}}$  in the NLO evolution. Our evolution code is explained for using it in one's studies on the fragmentation functions.

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