

Pulling and Pushing a Cargo With a Catalytically Active Carrier

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Catalytically active particles suspended in a liquid can move due to self-phoresis by generating solute gradients via chemical reactions of the solvent occurring at parts of their surface. Such particles can be used as carriers at the micro-scale. As a simple model for a carrier-cargo system we consider a catalytically active particle connected by a thin rigid rod to a catalytically inert cargo particle. We show that the velocity of the composite strongly depends on the relative orientation of the carrier-cargo link. Accordingly, there is an optimal configuration for the linkage. The subtlety of such carriers is underscored by the observation that a spherical particle completely covered by catalyst, which is motionless when isolated, acts as a carrier once attached to a cargo.

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Introduction. The increasing interest in the development of “lab on a chip” devices has led to a stringent need of scaling standard machinery down to micro- and nano-scales. This reduction in size has raised a number of challenging issues, such as to endow small objects with the capacity to perform autonomous, directional motion [1–4]. Towards this goal two main routes are pursued. The first one consists of designing artificial mechanical “swimmers” by mimicking the sophisticated locomotion strategies of natural micro-organisms such as *E. Coli* or *Spiroplasma* (see, e.g., Refs. [3, 5] and references therein). The second approach consists of transforming chemical free energy into mechanical work by employing phoretic mechanisms, i.e., motion induced by interfacial interactions [2, 4]. In the following we focus on this latter approach.

Several proposals for such catalytic self-propellers have already been tested experimentally (see, e.g., Refs. [1, 6–10] and Refs. [2, 4] for reviews). The underlying idea [1] is that an asymmetric decoration of the surface of a particle with a catalyst, which promotes an activated reaction in the surrounding liquid medium, leads to a non-uniform distribution of product molecules around the surface of the particle. This non-uniform distribution gives rise to particle motion through a variety of mechanisms [1, 6, 8, 10]. When the size of the particle is decreased towards the micron scale or below, viscous and surface forces start to dominate and inertia-based mechanisms such as bubble ejection propulsion become ineffective [3]. (However, alternative propulsion mechanisms based on bubble formation can remain active, as for the catalytically active tubes proposed in Ref. [10].) If the product molecules remain dissolved in the surrounding liquid medium, concentration gradients develop along the surface of the particle. It has therefore been argued [6, 11] that in such

cases the motion of the catalyst-covered active particle is phoretic, i.e., it results from the interfacial interactions between the particle and the non-uniformly distributed product molecules generated by the chemical reaction. Recent experimental [2, 6, 8–10, 12, 13], simulation [14, 15], and theoretical [11, 13, 14, 16–19] studies of such systems have contributed to a significantly improved understanding of this self-induced phoresis of isolated active particles.

One of the envisioned applications of such self-propellers is to use them as active carriers for colloidal transport and assembly [10, 20]. While in classic phoresis [21, 22] the concentration gradients are externally imposed and maintained, for self-phoresis the gradients are dynamically generated by the catalytic reaction occurring on parts of the particle surface. The interplay between these concentration gradients and the ensuing hydrodynamic flows not only powers the phoretic motion of such active particles, but also influences the effective interaction among each other, with nearby inert particles, or with bounding walls [16, 18]. Accordingly, the performance of such active particles as carriers is expected to depend strongly on these effective interactions.

Here we study a simple model for the transport of an inert particle, posing as a cargo, by an active diffusio-phoretic carrier ¹. The model consists of two spherical particles, with the surface of one of them partially covered by a catalyst and being connected by a thin rigid rod. Similar to previous studies [11, 16–19], we adopt the standard theory of diffusio-phoresis [21, 22] and derive, within the constraints of this approach [18], the velocity of the carrier-cargo composite for two distinct orientations of the link [see Figs. 1(a)-(b)]. The results show that the performance of the carrier, i.e., the resulting velocity of the composite system, strongly depends

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¹ “Diffusio-phoresis” is restricted here to phoresis in gradients of electrically neutral solutes (often also denoted as “chemo-phoresis”).

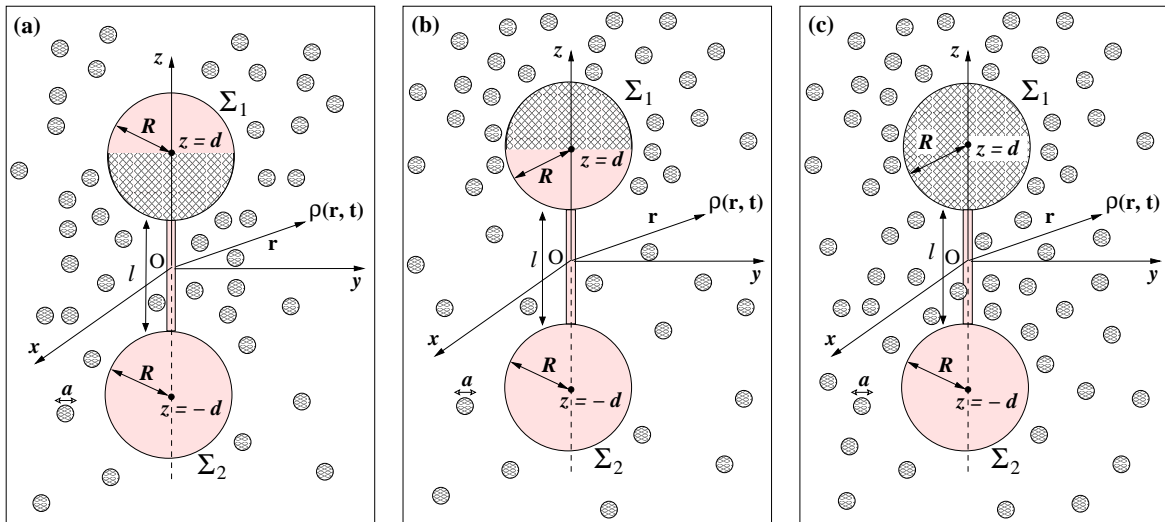


FIG. 1: Carrier-cargo system consisting of a hard spherical carrier (top circle) of radius R with its surface Σ_1 covered partially (a), (b) or completely (c) by a catalyst (hatched area) over a cap-like region. The carrier is linked via a thin rigid rod of length $l = 2(d - R)$ to a hard spherical, and inert cargo with surface Σ_2 and radius R . The product molecules (small hatched circles) with number density $\rho(\mathbf{r}, t)$ and of diameter a are emerging from the solvent (not shown) via a chemical reaction.

on the orientation of the link, which is a paradigmatic consequence of the self-phoresis mechanism of the motion. As an extreme case we study how a spherical particle, which is completely covered by catalyst and thus is unable to move on its own, can act as a carrier once it is attached to a cargo [see Fig. 1(c)]. We note that the emergence of motion in this latter case can be intuitively understood by realizing that in the limit of a very short linkage this configuration is equivalent with the so-called dimer model of an active particle [15].

Model. The system we consider is shown and characterized in Fig. 1. We assume a uniform distribution, with the areal density σ , of the catalyst over a hemisphere of the carrier particle. The infinitesimal thin rod enforces that there is no relative motion between the carrier and the cargo. Furthermore, the rod is aligned such that the carrier-cargo composite possesses axial symmetry. The co-moving coordinate system has its z direction along the axis of symmetry and the xy plane is the midplane between the two spheres. If the carrier is partially covered by catalyst, there are two possible configurations with axial symmetry: the active area of the carrier points towards [Fig. 1(a)] or away from [Fig. 1(b)] the cargo. For this system the only possible motion is a translation along the z -direction. The purpose of these simplifications is to sift out the main phenomena of interest, i.e., the dependence of the self-phoretic velocity on the internal orientation of the carrier-cargo system and, for the configuration shown in Fig. 1(c) (which can be seen as a dimer model like in Ref. [15]), the emergence of motion solely from linking together an otherwise motionless active particle with an inert cargo.

The catalyst promotes the chemical conversion of the solvent surrounding the composite system into product molecules. Here we focus on the particular case in

which the chemical conversion $A \xrightarrow{\text{cat}} A' + B$ of a solvent molecule (A) leads to two product molecules (A' and B) only, one with properties and size being similar to the solvent itself ($A' \approx A$), the other one (B) being significantly different². Accordingly, in the following only this latter one is denoted as a product molecule and plays the role of a solute in the solvent. The product molecules of diameter a diffuse into the solvent characterized by a diffusion coefficient D . Thus the net result of the chemical conversion can be viewed approximately as the generation of a solute only by an ensemble of independent sources uniformly distributed over a part of the carrier surface. The reaction rate ν_B at such a catalytic site, i.e., the number of product molecules created at that site per unit time t , is assumed to be independent of time. The number density $\rho(\mathbf{r}, t)$ of product molecules is considered to be so low that among themselves they behave like an ideal gas. However, there is an interaction potential between the product molecules and the moving particle, which, inter alia, realizes the impermeability condition at the particle surface. The interactions between the product molecules and the solvent are accounted for effectively via the Stokes - Einstein expression $D = k_B T / (3\pi\mu a)$ [23], where k_B is the Boltzmann constant, T is the temperature, and μ is the viscosity of the solution (i.e., solvent plus solute).

The direct and the solvent mediated particle-solute interactions combined with the non-uniform distribu-

² It has been argued that this is approximately the case for the Pt catalyzed decomposition in aqueous solution of hydrogen peroxide ($A = \text{H}_2\text{O}_2$) into water ($A' = \text{H}_2\text{O}$) and oxygen ($B = \text{O}_2$) [4, 8, 11, 19].

tion of the solute, created at the catalyst covered region, lead to an unbalanced osmotic pressure *along* the surface of the particle which induces flow of the solvent [11, 17, 18, 21, 22, 24] and motion of the particle. For micrometer-size particles typical self-phoretic velocities are of the order of $\mu\text{m/s}$. Accordingly, both the Reynolds number $\text{Re} \simeq \tilde{\rho}_{\text{solv}} \tilde{V} \tilde{R} / \mu$ (where $\tilde{\rho}_{\text{solv}}$ is the mass density of the solvent, \tilde{R} the linear extension of the particle, and \tilde{V} the velocity of the translational or rotational motion) and the Peclet number $\text{Pe} \simeq \tilde{V} \tilde{R} / D$ are small [25]. Thus the hydrodynamic description approximately reduces to the Stokes equations and the convection of the solute can be disregarded compared with its diffusive transport.

Phoretic slip. The effective interactions between the particles and the self-generated, asymmetric, non-uniform solute number density $\rho(\mathbf{r}, t)$ around the particles [16, 21, 22] have a typical range δ , which is comparable with the solute diameter a , and induce flow of the solution relative to the particle. In steady state this hydrodynamic flow in the thin surface layer $\sim \delta$ is accounted for by a (phoretic) slip-velocity [21, 22],

$$\mathbf{v}_s(\mathbf{r}_p) = -b(\mathbf{r}_p) \nabla^\Sigma \rho(\mathbf{r}_p), \text{ for } \mathbf{r}_p \in \Sigma (= \Sigma_1 \cup \Sigma_2), \quad (1)$$

where \mathbf{r}_p is a point P on the surface $\Sigma = \Sigma_1 \cup \Sigma_2$ of the particles and ∇^Σ denotes the projection of the gradient operator onto the corresponding local tangential plane of the surface of the particles³. This serves as a boundary condition for the hydrodynamic flow in the outer region, i.e., outside the surface layer [16, 18, 22]. The mobility coefficient $b(\mathbf{r}_p)$ is determined by the aforementioned effective interaction potential and by the hydrodynamic boundary condition (stick or slip) on the surface of the particle, which is the *inner edge* of the surface layer [22, 24]. For simplicity, here we take $b(\mathbf{r}_p)$ to be constant over the whole surface Σ . We note that $b \leq 0$ correspond to repulsive and attractive effective interactions, respectively [18, 22].

Distribution of product molecules. In the limit of small Peclet numbers and neglecting any so-called polarization effects of the surface layer [22], the steady state distribution $\rho(\mathbf{r})$ of product molecules in the outer region around the two moving particles is governed, in the co-moving frame, by the diffusion equation

$$D \nabla^2 \rho(\mathbf{r}) = 0, \mathbf{r} \in \text{outer region}. \quad (2)$$

This is subject to the boundary conditions (BCs)

$$\rho(|\mathbf{r}| \rightarrow \infty) = 0, \quad (3a)$$

$$-D [\hat{\mathbf{n}} \cdot \nabla \rho(\mathbf{r})] |_{\mathbf{r} \in \Sigma} = \nu_B \sigma \times \begin{cases} 1, & \mathbf{r} \in \text{catalyst} \\ 0, & \text{otherwise} \end{cases}. \quad (3b)$$

Equation (3b), where $\nu_B \sigma$ corresponds to the reaction rate per unit area and $\hat{\mathbf{n}}$ denotes the outward direction normal to the surface, describes how the catalytic reaction at $\mathbf{r} \in \Sigma$ translates into a source of product particles B [16, 19].

Hydrodynamic flow outside the surface layer. Because there are no forces acting on the solution beyond the surface layer, based on the assumption of low Reynolds numbers the hydrodynamic flow field \mathbf{u} in the outer region is obtained as the solution of force free and incompressible Stokes equations:

$$\nabla \cdot \hat{\Pi} = 0, \quad \nabla \cdot \mathbf{u} = 0. \quad (4)$$

$\hat{\Pi} := -p\hat{\mathbf{I}} + \mu\hat{\mathbf{S}}$ is the corresponding pressure tensor, where p is the hydrostatic pressure and $\hat{\mathbf{S}}$ is the shear stress tensor, i.e., $S_{\alpha\beta} = \partial u_\alpha / \partial x_\beta + \partial u_\beta / \partial x_\alpha$. In the comoving reference frame, attached to the carrier-cargo composite which is moving with $\mathbf{V} = V\hat{\mathbf{e}}_z$ relative to the solution, which is quiescent far away, these equations are subject to the BCs of a flow velocity $-\mathbf{V}$ far away ($|\mathbf{r}| \rightarrow \infty$) from the composite and $\mathbf{v}_s(\mathbf{r}_p)$ at the outer edge of the surface layer. This corresponds to sticking at the surface of the particles plus a slip velocity \mathbf{v}_s at the outer edge of the surface layer:

$$\mathbf{u}|_\Sigma = \mathbf{v}_s, \quad \mathbf{u}|_{|\mathbf{r}| \rightarrow \infty} = -\mathbf{V}. \quad (5)$$

Equation (5) reveals that the *cargo* plays an *active* role ($\mathbf{v}_s \neq 0$ on $\Sigma_2 \subset \Sigma$) despite being catalytically inert.

Phoretic velocity. After computing the hydrodynamic flow in the outer region, which depends parametrically on the translation of the two particles via the BCs in Eq. (5), the phoretic velocity \mathbf{V} is determined by the condition that the motion of the system composed of the particles plus their surface layers is force free [22].

Equations (2) and (3) as well as Eqs. (4) and (5) are most conveniently solved in terms of bispherical coordinates ($\xi \in \mathbb{R}, 0 \leq \eta \leq \pi, 0 \leq \phi < 2\pi$) [26–29]

$$\{x, y, z\} = \varkappa \{\sin \eta \cos \phi, \sin \eta \sin \phi, \sinh \xi\} / C, \quad (6)$$

where $C = \cosh \xi - \cos \eta$; the corresponding scale factors $h_\xi = |\partial \mathbf{r} / \partial \xi| = [(\partial x / \partial \xi)^2 + (\partial y / \partial \xi)^2 + (\partial z / \partial \xi)^2]^{1/2}$, $h_\eta = |\partial \mathbf{r} / \partial \eta|$, and $h_\phi = |\partial \mathbf{r} / \partial \phi|$ are given by

$$\{h_\xi, h_\eta, h_\phi\} = \varkappa \{1, 1, \sin \eta\} / C. \quad (7)$$

The choice $\varkappa = \sqrt{d^2 - R^2}$ ensures that the family of spheres $\xi = \text{const}$ includes the ones, $\xi = \pm \xi_0 := \pm \text{arccosh}(d/R)$, corresponding to the surfaces $\Sigma_{1,2}$ of the carrier and the cargo, respectively. Noting that the intersection of an η iso-surface with a ξ iso-surface is a circle parallel to the xy plane and that the equatorial circle parallel to the xy plane on Σ_1 corresponds to $\eta_0 = \text{arccotg}(R/\sqrt{d^2 - R^2})$, the area covered by the

³ Rigorously, Eq. (1) should be interpreted as a condition on the outer edge Σ_δ of the surface layer. For the outer problem this can be replaced by Σ because ρ varies over length scales which are much larger than δ .

catalyst is parametrized by $\xi = \xi_0$, $0 \leq \phi < 2\pi$, and $\eta_0 \leq \eta \leq \pi$ for the configuration in Fig. 1(a), $0 \leq \eta \leq \eta_0$ for the one in Fig. 1(b), and $0 \leq \eta \leq \pi$ for the one in Fig. 1(c).

In terms of bispherical coordinates the solution $\rho(\xi, \eta)$ of Eq. (2), which does not depend on ϕ due to the axial symmetry of the system, which is finite at $\eta = 0, \pi$ (i.e., on the z axis), and which satisfies the BC in Eq. (3a), can be written as [26, 27]

$$\rho(\xi, \omega := \cos \eta) = \rho_0 (\cosh \xi - \omega)^{1/2} \sum_{n \geq 0} P_n(\omega) \times [A_n \sinh((n+1/2)\xi) + B_n \cosh((n+1/2)\xi)], \quad (8)$$

where P_n denotes the Legendre polynomial of order n and $\rho_0 := R\nu_B\sigma/D$ is a density scale chosen such that the system specific parameters are factored out from the boundary conditions [Eqs. 3]. Noting that $\hat{\mathbf{n}} = (-, +)\hat{\mathbf{e}}_\xi = (+, -)\{\sinh \xi \sin \eta \cos \phi, \sinh \xi \sin \eta \sin \phi, \cosh \xi \cos \eta - 1\}/C$ on $\Sigma_{1,2}$ and expanding the right hand side of Eq. (3b) in a series of Legendre polynomials, the BCs in Eq. (3b) determine the coefficients $\{A_n, B_n\}$ as the solution of a system of linear equations. This determines $\rho(\xi, \eta)$ and the slip velocity follows from $\mathbf{v}_s = -[(b/h_\eta)\partial_\eta \rho(\xi, \eta)]_{\xi=\pm\xi_0} \hat{\mathbf{e}}_\eta$ with $\hat{\mathbf{e}}_\eta = \{(\cosh \xi \cos \eta - 1) \cos \phi, (\cosh \xi \cos \eta - 1) \sin \phi, -\sinh \xi \sin \eta\}/C$.

Due to the linearity of the Stokes equations the hydrodynamic flow field $\mathbf{u} = \mathbf{u}_I + \mathbf{u}_{II}$ [Eqs. (4) and (5)] is the superposition of the one corresponding to $\mathbf{u}_I(|\mathbf{r}| \rightarrow \infty) = -\mathbf{V}$ with stick BCs on Σ and the one corresponding to a quiescent flow far away, i.e., $\mathbf{u}_{II}(|\mathbf{r}| \rightarrow \infty) = 0$ with slip BCs \mathbf{v}_s on Σ . The solution for the first problem is known [28] and corresponds to a hydrodynamic force on the composite $\mathbf{F}_I = -12\pi\mu R\lambda\mathbf{V}$, where

$$\lambda = \frac{4}{3} \sinh \xi_0 \sum_{n \geq 1} \frac{n(n+1)}{(2n-1)(2n+3)} \times \left[1 - \frac{4 \sinh^2(n+1/2)\xi_0 - (2n+1)^2 \sinh^2 \xi_0}{2 \sinh(2n+1)\xi_0 + (2n+1) \sinh 2\xi_0} \right] \quad (9)$$

The second solution \mathbf{u}_{II} for the flow field is most conveniently expressed in terms of the Stokes stream function Ψ for axisymmetric flows [which in cylindrical coordinates $\{\tilde{r} = \sqrt{x^2 + y^2}, \phi, z\}$ is defined by $(u_{\tilde{r}}, u_z) := (-\partial_z \Psi, \partial_{\tilde{r}} \Psi)/\tilde{r}$]. In terms of bispherical coordinates $\Psi(\xi, \omega := \cos \eta)$ is given by [28]

$$\Psi(\xi, \omega) = V_0 R^2 \sum_{n \geq 0} \frac{W_n(\xi) C_{n+1}^{(-1/2)}(\omega)}{(\cosh \xi - \omega)^{3/2}}, \quad (10)$$

where

$$W_n(\xi) = a_n \cosh((n-1/2)\xi) + b_n \sinh((n-1/2)\xi) + c_n \cosh((n+3/2)\xi) + d_n \sinh((n+3/2)\xi), \quad (11)$$

$C_n^{(-1/2)}(\omega) = [P_{n-2}(\omega) - P_n(\omega)]/(2n-1)$ [28] is for-

mally denoted as the Gegenbauer polynomial of degree n and order $-1/2$ [30], and the characteristic velocity $V_0 = b\rho_0/R$ is chosen such that the system dependent parameters are factored out from the boundary conditions in Eq. (5). Because there are no flow sources or sinks along the z -axis, we require the stream function to vanish there [25], i.e., $\Psi(\xi, \omega = \pm 1) = 0$. Since $C_m^{(-1/2)}(\omega = \pm 1) = 0$ for $m \geq 2$, but as a linear function $C_1^{(-1/2)}(\omega)$ cannot be zero for both $\omega = \pm 1$, this constraint implies that the term $n = 0$ is removed from the series representation in Eq. (10).

In terms of the stream function, the boundary condition of a vanishing flow velocity along the direction normal to the surfaces $\Sigma_{1,2}$ (corresponding to impenetrability) leads to the requirement $[\partial \Psi(\xi, \omega = \cos \eta)/\partial \eta]_{\pm \xi_0} = 0$ [25], which can be shown to be equivalent to the simpler form $\Psi(\pm \xi_0, \omega) = 0$ [25, 30]. The flow velocity along the slip direction η is given in terms of the stream function by $u_\eta = -C^2 (\varkappa^2 \sin \eta)^{-1} \partial_\xi \Psi$ [25] which, according to Eq. (5), on the surfaces $\Sigma_{1,2}$ should be equal to the phoretic slip \mathbf{v}_s . Since for $n \neq m$ and $n, m \geq 2$ the polynomials $C_{n,m}^{(-1/2)}$ are orthogonal, $\int_{-1}^1 d\omega (1 - \omega^2)^{-1} C_n^{(-1/2)}(\omega) C_m^{(-1/2)}(\omega) = 0$, the coefficients $\{a_n, \dots, d_n\}$ can be determined from these boundary conditions on Ψ in terms of $\{A_n, B_n\}$ by solving a system of linear equations⁴. The hydrodynamic force acting in the positive z -direction on the composite due to this second flow \mathbf{u}_{II} is given by $F_{II} = (2^{5/2} \pi \mu V_0 R^2 / \varkappa) \sum_{n \geq 1} (a_n + c_n)$ [28].

Requiring that the total force $\mathbf{F}_I + \mathbf{F}_{II}$ acting on the composite vanishes [21, 22] thus leads to the following expression for the velocity:

$$V/V_0 = \frac{\sqrt{2}}{3\lambda\sqrt{(d/R)^2 - 1}} \sum_{n \geq 1} (a_n + c_n). \quad (12)$$

Discussion. In Fig. 2 we show the velocity of the carrier-cargo system as a function of the scaled length $l/R = 2(d/R - 1)$ of the linkage in the range $0.02 \leq l/R \leq 18$ for the three configurations considered in Fig. 1 in the case of *repulsive* effective interactions between the product molecules and the material forming the carrier-cargo system, i.e., for $b < 0$ and $V_0 < 0$. (The calculations can easily be extended to $l/R < 0.02$, but: (i) the implicit assumptions of a homogeneous solvent and point-like product molecules are expected to break down for very small separations, which renders Eq. (12) to be inapplicable for too small values of l/R , and (ii) the limiting configuration $l/R = 0$ correspond-

⁴ In practice, the infinite system has to be truncated at a certain order $n = N_{max}$. For our system it turns out that both A_n and B_n vanish rapidly upon increasing n . In all cases studied, at $N_{max} = 100$ these coefficients are smaller than 10^{-20} , compared with values of the order of unity for $n = 0$. This behavior is sufficient for the convergence of the velocity expression in Eq. (12).

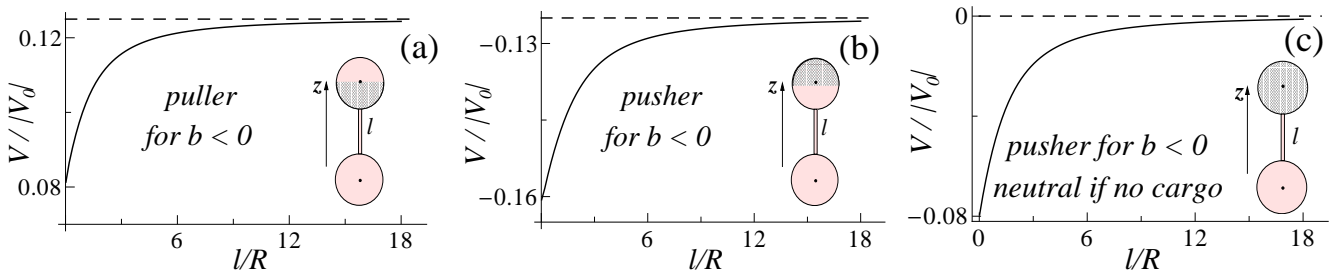


FIG. 2: The velocity V along the z -direction (indicated in the insets) in units of $|V_0|$ as a function of the scaled length $0.02 \leq l/R \leq 18$ of the linkage for the three configurations shown in the corresponding insets and for the case that the effective interaction between the product molecules and the two particles is repulsive ($b < 0$). The dashed lines in (a) and (b) correspond to the values $\pm|V_0|/8$, respectively, which the velocity of the cargo-carrier composite seems to attain as the cargo is linked at a larger distance from the carrier.

ing to carrier and cargo being in contact merely reduces to the case of self-diffusiophoresis of a single particle with a complex shape.)

For the choice $b < 0$ the carrier alone moves against the gradient of product molecule along its surface. Therefore the configurations in Figs. 1 (a) and (b) correspond to a pulling and a pushing carrier, respectively. Focusing first on the configurations in Figs. 2 (a) and (b), we note that the pusher or puller character is maintained at all separations l , i.e., the velocity of the composite is always along the positive and negative z direction in the cases (a) and (b), respectively. In all cases, for $l/R \lesssim 4$ the velocity shows a significant dependence on the separation l , which clearly indicates that the cargo plays actually an active role in the resulting motion of the composite. In both cases at large separations l the velocity approaches limiting values seemingly equal to $\pm|V_0|/8$, respectively, which is $1/2$ of the velocity at which the active carrier half-covered by catalyst would move if isolated [19]. However, the pusher slows down upon increasing l whereas the puller speeds up. Therefore, for any length l of the linkage the pusher configuration exhibits a faster motion than the puller one. These findings can be rationalized intuitively as follows. For example, in the case (a) the generation of product molecules by the carrier induces also a concentration gradient around the cargo surface pointing in the direction opposite to the one on the carrier surface. Consequently, the cargo behaves also like an active particle and induces a hydrodynamic flow around its surface in the direction opposite to the one around the carrier, which thus leads to a smaller net hydrodynamic flow and accordingly to a slower motion of the composite.

Any other orientation of the carrier-cargo link breaks the axial symmetry, inducing a rotation of the composite in addition to its translation; this leads to a reduction in the translational velocity. Therefore the pusher configuration [Fig. 1 (b)] is the optimal (i.e., maximal velocity) configuration if the effective interaction between the product molecules and the carrier-cargo material is repulsive. On the other hand, if this effective interaction is attractive ($b > 0$) the same intu-

itive arguments as above lead to the conclusion that the puller and pusher characters are interchanged between the configurations shown in Fig. 1(a) and (b), while the l -dependence of the velocity changes signs. Therefore, for attractive effective interactions the puller configuration [Fig. 1 (b)] is the optimal one.

The motion of active particles is known to be affected by thermal fluctuations, and thus its directionality only holds over time scales smaller than the characteristic rotational diffusion time, crossing over to Brownian motion at longer time scales [16, 31]. Inspecting the cases of the carrier-cargo configurations shown in Figs. 1 (a) and (b), one realizes that in (a) the cargo has a stronger influence than in (b) on the stability of the composite with respect to such fluctuations of the direction of motion. For $b < 0$, in the case of the puller [Fig. 1 (a)] a sudden change in direction producing a tilt of the symmetry axis towards the left relative to the Oz axis breaks the axial symmetry of the product concentration profile, and larger concentrations occur to the right of the symmetry axis. Consequently, right after the change in direction the cargo is driven through a region where the concentration of the product particles is larger on its right half (relative to the cargo-carrier axis) and thus induces a torque on the cargo and a rotation of the symmetry axis back towards the Oz direction. Therefore, in the puller configuration the cargo tends to stabilize the directionality of motion against thermal fluctuations. On the other hand, in the pusher configuration [Fig. 1 (b)] the cargo is further away from the source of product particles. Therefore it is basically insensitive to such changes in the symmetry of the product concentration distribution as it moves away from it and consequently no significant restoring torques occur.

Configuration (c) reveals the rather peculiar consequence of self-phoretic propulsion that a carrier, which in isolation would be motionless, is activated by being linked to an otherwise inert cargo. This occurs because the linkage provides the anisotropy needed for self-phoresis to become operational [6, 11]. For short links, the velocity of such a composite is significant. According to Fig. 2, for $l/R \lesssim 1$, $|V|/|V_0|$ is approximately $1/3$ of the largest possible velocity $|V_0|/4$ of

an isolated spherical active carrier. For repulsive (attractive) effective interactions the inert cargo turns the neutral carrier into a pusher (puller). We note that for lengths $l/R \ll 1$ the carrier-cargo system in configuration (c) becomes similar to the geometry of the so-called dimer model of an active colloid which, for an $A \rightarrow B$ catalytic reaction, has been proposed and investigated with Molecular Dynamics simulations [15].

The diffusiophoresis mechanism and the geometry of the model have been chosen with the intention to provide clear examples which reveal and underscore the complexity of such active carrier - cargo systems. We note that the main influence of the inert cargo stems from the fact that the nearby chemically active colloid gives rise to concentration gradients, and thus to phoretic slip velocity, along its surface, too. This is very different from the cases discussed in Ref. [32], where hydrodynamic interactions between dimer swimmers are "rectifying" the otherwise reciprocal movement of each of two dimers, and thus are leading to the emergence of collective and relative motion. We anticipate a rather rich behavior to emerge as various model constraints are

relaxed, such as: (i) Different effective interactions between the product molecules and the cargo and carrier material, i.e., different mobility factors b (of potentially opposite sign) on the carrier and cargo surfaces, will lead to a complex dependence of the velocity on the orientation of the linkage. (For example, in the case shown in Fig. 2(a) with $b_{1,2}$ of opposite sign the velocity can change sign as $|b_2|$ is increased.) (ii) In the case of charged active particles and charged reaction products, the motion will be determined by the interplay of self-diffusiophoresis and self-electrophoresis, which amplifies the roles played by the orientation of the linkage and by the surface properties of the cargo and carrier. (iii) A convex or concave shape of the surface of the cargo facing the carrier side leads to a possible amplification or reduction, respectively, of the concentration gradients around the carrier and the cargo. This list can be extended, but it already now shows that employing active particles as carriers allows an exceptional flexibility in the design of cargo-carrier systems, which should be very beneficial for potential applications.

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