



## Abstract View

[Volume 13, Issue 8 \(August 1983\)](#)

### Journal of Physical Oceanography

Article: pp. 1383–1397 | [Abstract](#) | [PDF \(959K\)](#)

# The Free Kelvin Wave in Finite-Difference Numerical Models

**William W. Hsieh, Michael K. Davey, and Roxana C. Wajswicz**

*Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge Cambridge CB3 9EW, U.K.*

(Manuscript received January 20, 1983, in final form May 16, 1983)

DOI: 10.1175/1520-0485(1983)013<1383:TFKWIF>2.0.CO;2

### ABSTRACT

The effects of viscosity and finite-differencing on free Kelvin waves in numerical models (which employ the Arakawa *B*- or *C*-grid difference schemes) are investigated using the *f*-plane shallow-water equations with offshore finite-difference grids, (assuming alongshore geostrophy). Three nondimensional parameters arise:  $\Delta$  [= (offshore grid spacing)/(Rossby radius)],  $\epsilon$  characterizes the offshore lateral viscous effect and  $\alpha$  the combined vertical and alongshore viscous effect. This study is more relevant to *baroclinic* Kelvin waves which tend to suffer poor offshore resolution because of their small Rossby radii.

For inviscid models ( $\epsilon = \alpha = 0$ ), as  $\Delta$  increases (resolution worsens), the alongshore speed increases dramatically in the *B*-grid, but stays constant at the gravity wave speed in the *C*-grid. Models with damping only ( $\alpha > 0$ ,  $\epsilon = 0$ ) behave similarly. With lateral viscosity ( $\epsilon > 0$ ,  $\alpha > 0$ ), increasing  $\epsilon$  decreases the speed in both the *B*- and *C*-grids—the drop in speed being less severe when the free-slip boundary condition is imposed instead of the no-slip one. As  $\Delta$  increases, the speed declines in the *B*-grid, but in the *C*-grid, worsening resolution cancels the viscous slow-down, with speed rising to that when  $\epsilon = 0$ .

Our theory predicts the alongshore phase speed, the temporal decay rate and the offshore structure for *B*- and *C*-grid models of given viscosity and grid-spacing and of given boundary conditions (e.g., no-slip or free-slip). The predictions are checked against observations from two- and three-dimensional model—including the Bryan-Cox model—with good agreement.

#### Options:

- [Create Reference](#)
- [Email this Article](#)
- [Add to MyArchive](#)
- [Search AMS Glossary](#)

#### Search CrossRef for:

- [Articles Citing This Article](#)

#### Search Google Scholar for:

- [William W. Hsieh](#)
- [Michael K. Davey](#)
- [Roxana C. Wajswicz](#)



© 2008 American Meteorological Society [Privacy Policy and Disclaimer](#)

Headquarters: 45 Beacon Street Boston, MA 02108-3693

DC Office: 1120 G Street, NW, Suite 800 Washington DC, 20005-3826

[amsinfo@ametsoc.org](mailto:amsinfo@ametsoc.org) Phone: 617-227-2425 Fax: 617-742-8718

[Allen Press, Inc.](#) assists in the online publication of *AMS* journals.