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## Linear Problems of Optimal Control of Fuzzy Maps

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### ABSTRACT

In the present paper, we show the some properties of the fuzzy R-solution of the control linear fuzzy differential inclusions and research the optimal time problems for it.

### KEYWORDS

fuzzy differential inclusions, control problems

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