

# Optimal maintenance policy for a system subject to damage in a discrete time process

### Yu-Hung Chien<sup>a,</sup> 📥 · 🖾, Shey-Huei Sheu<sup>b, c</sup>, Zhe George Zhang<sup>d, e</sup>

a Department of Applied Statistics, National Taichung University of Science and Technology, No. 129, Section 3, San-min Road, North District, Taichung 40401, Taiwan

b Department of Statistics and Informatics, Providence University, No. 200, Chung Chi Road, Taichung 43301, Taiwan

 Department of Industrial Management, National Taiwan University of Science and Technology, No. 43, Section 4, Keelung Road, Taipei 107, Taiwan

d Department of Decision Sciences, Western Washington University, 516 High Street, Bellingham, WA 98225, USA

e Beedie School of Business, Simon Fraser University, Burnaby, BC, Canada V5A 1S6

http://dx.doi.org/10.1016/j.ress.2012.03.002, How to Cite or Link Using DOI

View full text

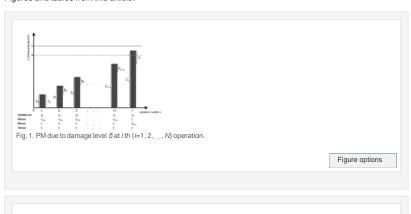
Purchase \$41.95

## Abstract

Consider a system operating over *n* discrete time periods (*n*=1, 2, ...). Each operation period causes a random amount of damage to the system which accumulates over time periods. The system fails when the cumulative damage exceeds a failure level  $\zeta$  and a corrective maintenance (CM) action is immediately taken. To prevent such a failure, a preventive maintenance (PM) may be performed. In an operation period without a CM or PM, a regular maintenance (RM) is conducted at the end of that period to maintain the operation of the system. We propose a maintenance policy which prescribes a PM when the accumulated damage exceeds a pre-specified level  $\delta$  (< $\zeta$ ), or when the number of operation periods reaches *N*, whichever comes first. With the long-term average cost rate as an optimality criterion, we optimize the maintenance policy parameters  $\delta$  and *N* and discuss some useful properties about them. It has been shown that a  $\delta$ -based PM outperforms a N-based PM in terms of cost minimization. Numerical examples are presented to demonstrate the optimization of this class of maintenance policies.

## Keywords

Maintenance; Cumulative damage; Expected cost rate; Operation period; Renewal reward theory



### Figures and tables from this article:

$\mathbf{Fig. 2. CM}$ due to damage level $\zeta$ at <i>i</i> th ( <i>i</i> =1, 2,, N) operation.	
	Figure options
Fig. 3. PM due to the completion of <i>N</i> th operation without exceeding damage level δ.	
	Figure options
	J
Table 1-1. <i>N</i> and <i>CR</i> ( $\delta$ , <i>N</i> ) for a given $\delta$ =20 and under $\zeta$ =20, <i>C</i> <sub>pu</sub> =10, and <i>c</i> <sub>m</sub> = <i>c</i> <sub>0</sub> =1.	
Table 1-2. N and $CR(\delta,N)$ for a given $\delta$ =18 and under $\zeta$ =20, $C_{\rho_M}$ =10, and $c_m$ = $c_0$ =1.	
Table 1-3. <i>N</i> and <i>CR</i> ( $\delta$ , <i>N</i> ) for a given $\delta$ =16 and under $\zeta$ =20, <i>C</i> <sub>pu</sub> =10, and <i>c</i> <sub>m</sub> = <i>c</i> <sub>0</sub> =1.	
Table 1-4. <i>N</i> and <i>CR</i> ( $\delta$ , <i>N</i> ) for a given $\delta$ =14 and under $\zeta$ =20, <i>C</i> <sub>pM</sub> =10, and <i>c</i> <sub>m</sub> = <i>c</i> <sub>0</sub> =1.	
Table 2-1. $\delta$ and $CR(\delta, N)$ for a given $N=\infty$ and under $\zeta=20$ , $C_{pu}=10$ , and $c_m=c_0=1$ .	
Table 2-2. $\delta$ and $CR(\delta, N)$ for a given $N=15$ and under $\zeta=20$ , $C_{\rho_M}=10$ , and $c_m=c_0=1$ .	
Table 2-3. $\delta$ and $CR(\delta, N)$ for a given $N=10$ and under $\zeta=20$ , $C_{_{PM}}=10$ , and $c_{_{mn}}=C_{_{0}}=1$ .	
Table 2-4. $\delta$ and $CR(\delta, N)$ for a given N=8 and under $\zeta$ =20, $C_{pu}$ =10, and $c_m = c_0 = 1$ .	

View Within Article

Table 2-5. $\delta$ and $CR(\delta, N)$ for a given $N=5$ and under $\zeta=20$ , $C_{_{PM}}=10$ , and $c_{_{m}}=c_{_{0}}=1$ .

Corresponding author. Tel.: +886 4 22196080; fax: +886 4 22196331. Copyright©2012 Elsevier Ltd. All rights reserved.