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## Implementing 4-Dimensional GLV Method on GLS Elliptic Curves with $j$ -Invariant 0

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**Abstract:** The Gallant-Lambert-Vanstone (GLV) method is a very efficient technique for accelerating point multiplication on elliptic curves with efficiently computable endomorphisms. Galbraith, Lin and Scott (J. Cryptol. 24(3), 446-469 (2010)) showed that point multiplication exploiting the 2-dimensional GLV method on a large class of curves over  $\text{GF}(p^2)$  was faster than the standard method on general elliptic curves over  $\text{GF}(p)$ , and left as an open problem to study the case of 4-dimensional GLV on special curves (e.g.,  $j(E) = 0$ ) over  $\text{GF}(p^2)$ . We study the above problem in this paper. We show how to get the 4-dimensional GLV decomposition with proper decomposed coefficients, and thus reduce the number of doublings for point multiplication on these curves to only a quarter. The resulting implementation shows that the 4-dimensional GLV method on a GLS curve runs in about 0.78 the time of the 2-dimensional GLV method on the same curve and in between 0.78-0.87 the time of the 2-dimensional GLV method using the standard method over  $\text{GF}(p)$ . In particular, our implementation reduces by up to 27% the time of the previously fastest implementation of point multiplication on x86-64 processors due to Longa and Gebotys (CHES2010).

**Category / Keywords:** public-key cryptography / Elliptic curves, point multiplication, GLV method, GLS curves.

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