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A low-memory algorithm for finding short product representations in finite groups

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Abstract: We describe a space-efficient algorithm for solving a generalization of the subset sum problem in a finite group G , using a Pollard-rho approach. Given an element z and a sequence of elements S , our algorithm attempts to find a subsequence of S whose product in G is equal to z . For a random sequence S of length $d \cdot \log_2(n)$, where $n = \#G$ and $d \geq 2$ is a constant, we find that its expected running time is $O(\sqrt{n} \cdot \log(n))$ group operations (we give a rigorous proof for $d > 4$), and it only needs to store $O(1)$ group elements. We consider applications to class groups of imaginary quadratic fields, and to finding isogenies between elliptic curves over a finite field.

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