



## Computing Discrete Logarithms in an Interval

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The discrete logarithm problem in an interval of size  $N$  in a group  $G$  is: Given  $g, h \in G$  and an integer  $N$  to find an integer  $0 \leq n \leq N$ , if it exists, such that  $h = g^n$ . Previously the best low-storage algorithm to solve this problem was the van Oorschot and Wiener version of the Pollard kangaroo method. The heuristic average case running time of this method is  $(2 + o(1)) \sqrt{N}$  group operations.

We present two new low-storage algorithms for the discrete logarithm problem in an interval of size  $N$ . The first algorithm is based on the Pollard kangaroo method, but uses 4 kangaroos instead of the usual two. We explain why this algorithm has heuristic average case expected running time of  $(1.714 + o(1)) \sqrt{N}$  group operations. The second algorithm is based on the Gaudry-Schost algorithm and the ideas of our first algorithm. We explain why this algorithm has heuristic average case expected running time of  $(1.660 + o(1)) \sqrt{N}$  group operations. We give experimental results that show that the methods do work close to that predicted by the theoretical analysis.

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