

## Exponential bounds for multivariate self-normalized sums

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### Abstract

In a non-parametric framework, we establish some non-asymptotic bounds for self-normalized sums and quadratic forms in the multivariate case for symmetric and general random variables. These bounds are entirely explicit and essentially depend in the general case on the kurtosis of the Euclidean norm of the standardized random variables.

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